

January 27-29, 2023

Ankara, Türkiye

**5. INTERNATIONAL ANKARA  
MULTIDISCIPLINARY STUDIES  
CONGRESS**

**ABSTRACT BOOK**



Edited by  
**Prof. Dr. Memet ŞAHİN**

**ISBN: 978-625-6404-52-6**

**[www.izdas.org](http://www.izdas.org)**

**NONSTATIONARY TEMPERATURE FIELDS AND THERMAL STRESSES IN A  
MULTILAYER AIRCRAFT GLAZING**

*Natalia Smetankina, Doctor of Technical Sciences*

*Anatolii Pidgorny Institute of Mechanical Engineering Problems  
of the National Academy of Sciences of Ukraine, Kharkiv, Ukraine*

*ORCID: 0000-0001-9528-3741*

*Serhii Misiura, PhD*

*Anatolii Pidgorny Institute of Mechanical Engineering Problems  
of the National Academy of Sciences of Ukraine, Kharkiv, Ukraine*

*ORCID: 0000-0002-5048-1610*

*Ievgeniia Misiura, PhD*

*Simon Kuznets Kharkiv National University of Economics, Kharkiv, Ukraine*

*ORCID: 0000-0002-5208-0853*

**ABSTRACT**

The majority of publications devoted to thermal stressed state of laminated structures deal with deformation of structures under steady temperature conditions or dynamic temperature fields with prescribed distribution through the thickness [1].

The hypothesis about a piecewise-linear temperature distribution through the thickness of a laminated package is often applied [2]. However, the non-stationary character of a problem requires a more exact description of the temperature field obtained directly from solution of a heat conduction equation [3-5].

A method for calculation of nonstationary thermal fields in a multilayer glazing of vehicles under the effect of impulse film heat sources is offered. The multilayer glazing is considered as a multilayer plate with complex shape made up of isotropic layers with constant thickness. The temperature on the side surface of the plate is zero. Convective heat transfer occurs on outer surfaces of the plate; on layers' interfaces film heat sources are arranged.

The heat conduction equation for an arbitrary plate layer after the Laplace transformation on time is reduced to the functional equation. In the same way initial and boundary conditions are transformed. A solution of the functional equation we search in the form of three space functions product. That enables us to get the system of ordinary differential equations. We represent the system solution as double trigonometrical series taking into account boundary conditions on the plate side surface.

Series expansion factors are determined from a system of linear algebraic equations which is formed of boundary conditions on outer surfaces and layers' interfaces. The system right member contains factors of expansion of interlayer film heat source functions. After determination of factors a transform of the required function is found by the second expansion theorem, and the problem solution has the form of double trigonometrical series.

Deformation of the plate is considered on the basis of the refined theory of the first-order accounting transverse shear strains in each layer. The thermal elastic equilibrium equations and the boundary conditions on the contour are obtained using Lagrange's variation principle. The problem solution is obtained by the embedding method [6]. According to the method, the complex-shape plate is virtually embedded within an auxiliary enveloping multilayer simply supported plate of rectangular planform shape with the same composition of layers. An auxiliary plate is one whose contour shape and boundary conditions yield a simple analytical solution. The system of general equations is integrated by expansion into Taylor series.

As an example, we investigated thermal fields and stresses in five-layer aircraft elements under heating by the film heat source. The heat source has the rectangular form. It is arranged between the first and the second layers of the glazing element. The stresses in glazing layers are determined under the action of heat fields obtained by solving the nonstationary heat conduction problem. The results were validated by comparison with test data [7].

The method offered can be used for designing a safe multilayer glazing of transport vehicles and different composite structures [8-14] under operational and emergency thermal loads.

### References

1. Swaminathan K., Sangeetha D.M. Thermal analysis of FGM plates – A critical review of various modeling techniques and solution methods. *Composite Structures*. 2017. Vol. 160. P. 43–60. <https://dx.doi.org/10.1016/j.compstruct.2016.10.047>
2. Guo Y., Jiang Y., Wang J., Huang, B. 3D thermal stresses in composite laminates under steady-state through-thickness thermal conduction. *Int. J. Applied Mechanics*. 2020. Vol. 12, No. 6, P. 2050065. <https://doi.org/10.1142/S1758825120500659>
3. Smetankina N.V., Postnyi O.V., Merkulova A.I., Merkulov D.O. Modeling of non-stationary temperature fields in multilayer shells with film heat sources. In: 2020 IEEE KhPI Week on Advanced Technology (KhPIWeek). 2020. P. 242–246. <https://doi.org/10.1109/KhPIWeek51551.2020.9250139>
4. Kantor B.Ya., Smetankina N.V., Shupikov A. N. Analysis of non-stationary temperature fields in laminated strips and plates. *Int. J. Solids Structures*. 2001. Vol. 38, No. 48/49. P. 8673–868 [https://doi.org/10.1016/S0020-7683\(01\)00099-3](https://doi.org/10.1016/S0020-7683(01)00099-3)
5. Shupikov A.N., Smetankina N.V., Svet Ye.V. Nonstationary heat conduction in complex-shape laminated plates. *Trans. ASME. Journal of Heat Transfer*. 2007. Vol. 129, No. 3. P 335–341. <https://doi.org/10.1115/1.2427073>
6. Smetankina N., Merkulova A., Merkulov D., Postnyi O. Dynamic response of laminate composite shells with complex shape under low-velocity impact. *Integrated Computer Technologies in Mechanical Engineering-2020. Lecture Notes in Networks and Systems*. 2021. Vol. 188. Springer, Cham. P. 267–276. [https://doi.org/10.1007/978-3-030-66717-7\\_22](https://doi.org/10.1007/978-3-030-66717-7_22)
7. Smetankina N., Merkulova A., Merkulov D., Misura S., Misiura Ie. Modelling thermal stresses in laminated aircraft elements of a complex form with account of heat sources. *ICoRSE 2022. Lecture Notes in Networks and Systems*. 2023. Vol. 534. Springer, Cham. P. 233–246. [https://doi.org/10.1007/978-3-031-15944-2\\_22](https://doi.org/10.1007/978-3-031-15944-2_22)
8. Shupikov A.N., Smetankina N.V., Sheludko H.A. Selection of optimal parameters of multilayer plates at nonstationary loading. *Meccanica*. 1998. Vol. 33, No 6. P. 553–564. <https://doi.org/10.1023/A:1004311229316>
9. Misura S., Smetankina N., Misiura Ie. Optimal design of the cyclically symmetrical structure under static load. *Integrated Computer Technologies in Mechanical Engineering-2020. Lecture Notes in Networks and Systems*. 2021. Vol. 188. Springer, Cham. P. 256–266. [https://doi.org/10.1007/978-3-030-66717-7\\_21](https://doi.org/10.1007/978-3-030-66717-7_21)
10. Alyokhina S., Kostikov A., Smetankina N., Gontarovskiy P., Garmash N., Melezhyk I. Methodology for determining the thermal and thermal-stress states of a concrete storage container for spent nuclear fuel for assessment of its service life. *Nuclear and Radiation Safety*. 2021. Vol. 4., No. 6. P. 33–39. [https://doi.org/10.32918/nrs.2021.4\(92\).05](https://doi.org/10.32918/nrs.2021.4(92).05)
11. Strelnikova E., Gnitko V., Krutchenko D., Naumenko Y. Free and forced vibrations of liquid storage tanks with baffles. *J. Modern Technology and Engineering*. 2018. Vol. 3. No.1. P.15–52.
12. Sierikova E. Strelnikova E. Gnitko V. Kryutchenko D. Reservoirs seismic resistance. *Proceedings book of 6th International Congress on Innovative Scientific Approaches*. December 19-20, 2021, Samsun, Turkey. IKSAD GLOBAL Publishing House. 2021. P. 264-267.

13. Sierikova O.M., Strelnikova O.O., Gnitko V.I., Tonkonozhenko A.M., Pisia L.A. Neutralization of static electricity in oil storage systems through application of nanocomposites with carbon fiber inclusions. Applied questions of mathematical modeling. 2021. Vol. 4, No. 2.2. P. 159–168. <https://doi.org/10.32782/KNTU2618-0340/2021.4.2.2.16>

14. Sierikova E., Strelnikova E., Pisia L. The environmental safety level increasing of oil storage Systems. Proc. of International Afghanistan Interdisciplinary Research Conference. Taj Institute of Higher Education Mazar-i-Sharif, Afghanistan. August 19, 2021. P. 286-288.